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Optimization of Blade Profiles of Cross Flow Turbine (CFT)

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Abstract

The areas where the supply of grid power is very difficult, Cross Flow Turbines (CFT) are used for low head power production. Results are presented for optimum profile of the leading edges of blade. Four different profiles (Flat tip blade profile, round tip blade profile, pointed tip blade profile and oval tip blade profile) are modeled and simulated with ANSYS CFX and then compared their performance in terms of their efficiencies. The complete turbine is analyzed for the determination of the leading edge of the blade in the first stage and the trailing edge in the second stage. The design and simulation conditions are based on the installed CFT at Chitral city of Pakistan. The results show that efficiency of the round tip blade profile is better than the other three profiles of the blade.

Keywords: Blade Profiles, Cross Flow Turbine (CFT), Turbine Efficiency, Renewable Energy, Hydro-Power

Biographical notes:

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Assad Zafar, Bilal Ibrahim and M. Awais Sarwar received his B.S in Mechanical Engineering from GIK Institute of Engineering Sciences and Technology. Currently, they are working in the industries.

1. Introduction

Pakistan has a hydro potential of approximately 42,000MW; however only 7,000MW is being utilized for electrical power production. Out of 42,000MW, micro hydro potential is about 1,300MW. The recoverable potential in micro-hydropower is roughly estimated to be 300MW on perennial water falls in northern Pakistan [1, 2]. For typical site conditions (available flow rate and head) in Pakistan, Cross Flow Turbines (CFTs) are best suited for medium head 5-150 m for micro-hydro power production [3]. This power developed can be along riverside. Cross flow turbine is the most widely used turbine for micro-hydro power plants. Because of the convenient in manufacturing, cheap maintenance and high efficiency make it an attractive choice for the manufacturers as well as investors [4]. The design specifications of CFT involves outer to inner diameter ratio, angle of attack (α), nozzle entry arc angle (λ), jet thickness to penstock width ratio (B/S_o), number of blades of runner, blade inlet angle, and blade exit angle.

The comprehensive literature on CFT design research has already been conducted. However, a very little work is done on the blade profiles of the runner. That's why the blade profile parameter is selected and CFD analysis of the complete turbine was done to study the effect on the efficiency of CFT. Before selecting this parameter to be considered, extensive literature review is carried out.

Through experimental research and analysis, much improvement in the design of the cross flow turbine has already been done since its advent. Experimental results published by different researchers have been presented in the literature. Khosrowpanah [5] tested four runners of 6 inches width. The nozzle was 6 inches wide. Water was entering vertically instead of entering horizontally or at an angle over the nozzle with nozzle entry arc of 58° , 78° and 90° . It was concluded that the increase in the nozzle entry arc and the runner diameter aspect ratio and a decrease in the number of blades results into the increase in the discharge of CFT. He concluded that number of blades should be 15 for the best efficiency for a runner diameter of 12 inches. Nakase et al. [6] studied the effect of nozzle shape on the performance of the Cross Flow Turbines by using the blade inlet and outlet angles of 30° and 90° with runner outer diameter of 315 mm. The runner had 26 blades. He classified the flow into two stages. The term crossed flow was coined for water that flows through both the stages. And that passed only first stage was termed as uncrossed

flow. The conclusion was made that nozzle throat width ratio ($2S_0/D\lambda$) of 0.26 is more efficient. Hara and Aziz [7] studied the effect of increasing the number of blades and concluded that highest efficiency is obtained when numbers of blades are in the vicinity of 35 with an angle attack of 22. The experiments were performed on nozzle width of 6 inches and 4 inches. They also reported that the blade exit angle of 55° was also reported in maximum efficiency. They also studied the effect of increasing the number of blades from 20 to 40. Fukutomi et al. [8] focused on the flow along the runner entrance and unsteady forces on the blades by investigating through 2D numerical calculations inside the runner (unsteady flow). Kaunda et al. [9] investigated the performance of CFT in terms of pressure drop, hydraulic efficiency and turbine efficiency at various turbine speeds. They concluded that CFT can be operated both at impulse and reaction principles. On the other hand, Choi et al. [4] performed an entire 2D CFD steady state cross flow turbine simulation, considering both water and water air flow conditions. With this approach, the authors studied the influence of nozzle shape, runner blade angle and runner blade number on the turbine performance. Moreover, the numerical calculations for important role of air layer were verified. Andrade et al. [10] showed that it was possible to simulate the behavior of the 3D steady state free surface flow (water-air) inside the nozzle casing assembly of the turbine by using CFD techniques. They obtained the flow angles along the nozzle outlet α_1 that would come into the first stage of the runner, slightly varies from 23° to 7° along the rotation angle θ . The deviation of the angle $\alpha_1 = 16^\circ$. The deviation of the α_1 angle is explained with the potential flow condition assumed when the nozzle is designed. In their study the numerical efficiency came out to be greater than the experimental one and the reason was attributed to not including the effect of the mechanical efficiency at high runner speeds in the numerical study.

2. Site Conditions

This study is based on the turbine which is currently installed in Chitral city in Pakistan by Hydrolinks [11]. The site conditions are as follows:

Table 1: Site conditions

Head	9.3 m
Flow Rate	0.45 m ³ /s

The turbine parameters are as following:

Table 2: Parameters selected for Cross Flow turbines

Runner Diameter	300 mm
Length of runner	420 mm
Runner rpm	386 rpm
Angle of attack (α)	22°
Outer to inner diameter ratio	0.68
Nozzle entry arc angle (λ)	90°
Jet thickness to penstock width ratio (B/S_o)	3.5
Number of blades	35
Shaft Diameter	50 mm

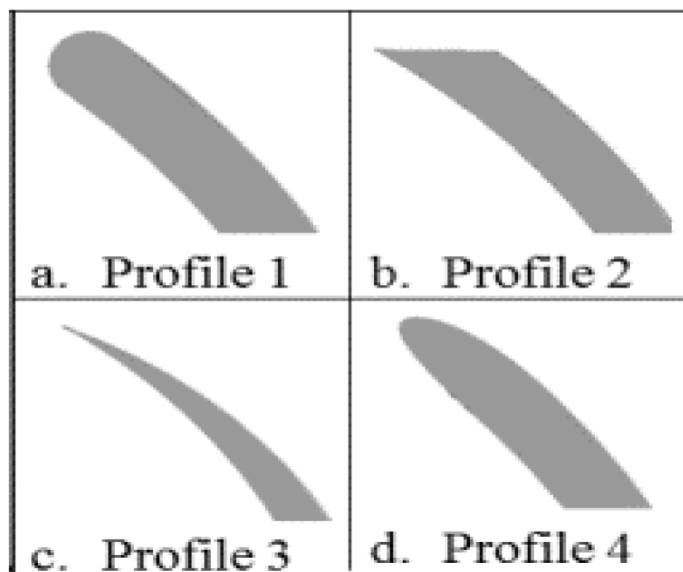


Fig. 2: a. Round Profile, b. Flat profile, c. Pointed Tip Profile, d. Oval profile

We have selected four different blade profiles for our CFD analysis which are shown in figure 2. **Profile 1** has a circular geometry tangent to three sides, 2 blade curves and the D1 of the rotor. **Profile 2** is sharp cut at the D1. **Profile 3** makes a pointed tip at the inner curve of the blade. **Profile 4** has an oval shape with the major diameter twice the minor diameter and the minor diameter equal to the blade thickness.

3. Model Development

The force from the water jet of initial velocity V_i can be calculated as below, if the blade is considered stationary:

$$F_x = m \times (V_i - V_f \cos \alpha)$$

$$F_y = m \times (0 - V_f \sin \alpha)$$

$$F_y = -m \times V_f \sin \alpha$$

Where V_i : Initial absolute velocity of water

V_f : Final absolute velocity of water

m: mass flow-rate of water

α = blade angle

Whereas the resultant force is calculated as follows:

$$F = \sqrt{F_x^2 + F_y^2}$$

$$F = \sqrt{[m \times (V_i - V_f \cos \alpha)]^2 + [m \times V_f \sin \alpha]^2}$$

$$F = m \times \sqrt{V_i^2 + V_f^2 \cos^2 \alpha - 2V_i V_f \cos \alpha + V_f^2 \sin^2 \alpha}$$

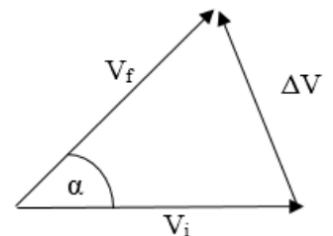
$$F = m \times \sqrt{V_i^2 + V_f^2 (\cos^2 \alpha + \sin^2 \alpha) - 2V_i V_f \cos \alpha}$$

$$F = m \times \sqrt{V_i^2 + V_f^2 - 2V_i V_f \cos \alpha}$$

$$F = m \times \sqrt{\Delta V^2}$$

$$\therefore (\cos^2 \alpha + \sin^2 \alpha) = 1$$

$$\therefore \Delta V^2 = V_i^2 + V_f^2 - 2V_i V_f \cos \alpha \quad (\text{By law of cosines})$$



$$F = m \times \Delta V$$

The power delivered can be calculated as:

$$P = F \times V$$

Power delivered to CFT by water will be in two components:

- Firstly, at inlet section of runner
- Secondly, at outlet section of runner

The power produced at inlet section can be calculated as:

$$T = m \times rV$$

$$P_1 = T_1 \times w$$

Where, w = angular velocity of runner

T = Torque produced by runner shaft

Total power delivered by runner shaft will be:

$$P = P_1 + P_2$$

$$P = m \times [(V_1 \cos \alpha_1) + (V_2 \cos \alpha_1)] \times u_1$$

$$P = m \times [(V_1 \cos \alpha_1) + (V_2 \cos \beta_2) - u_1] \times u_1$$

The relative velocities of water at inlet and outlet are related as:

$$v_2 = \psi \times v_1$$

$\Psi \approx 0.98$ = empirical co-efficient (to neglect the increase in velocity due to difference in height of upper and lower blades)

$$P = m ((V_1 \cos \alpha_1) + (\psi v_1 \cos \beta_2) - u_1) \times u_1$$

$$P = m ((V_1 \cos \alpha_1) + (\psi \times \frac{(V_1 \cos \alpha_1) - u_1}{\cos \beta_1} \cos \beta_2) - u_1) u_1$$

$$P = m [((V_1 \cos \alpha_1) - u_1) (1 + (\psi \times \frac{\cos \beta_2}{\cos \beta_1}))] u_1$$

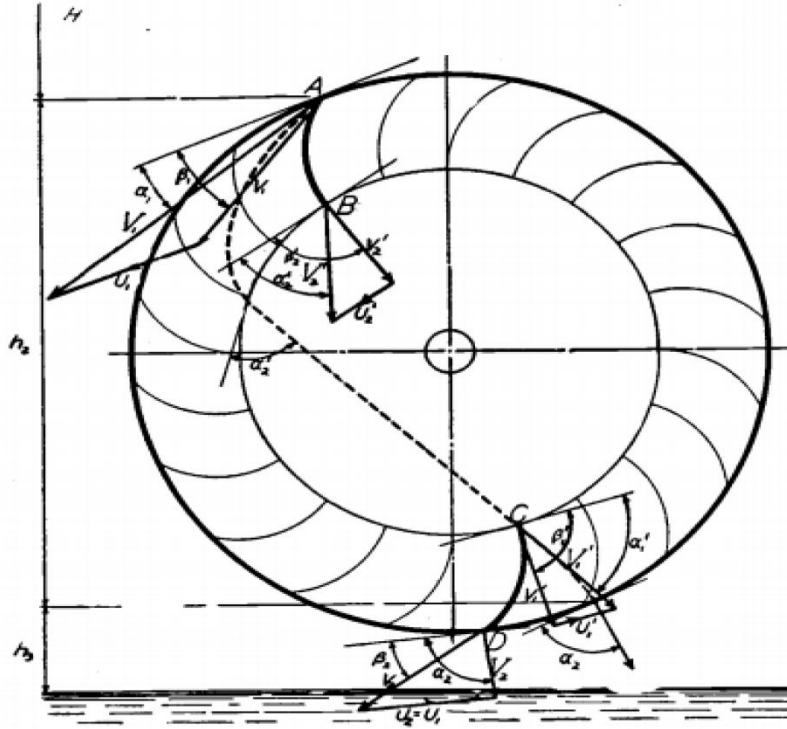


Fig. 3 velocity Triangle

Calculation for Input Power:

The theoretical power input due to head 'H' to a CFT can be calculated as:

$$P_i = \gamma \times Q \times H$$

$$V_1 = C \times \sqrt{2gH}$$

$$H = \frac{V_1^2}{2g + c^2}$$

C = Nozzle discharge co-efficient ~0.98

G= gravitational acceleration

Q = volumetric flow rate of water through CFT runner

Suing the above equations

$$P_i = \frac{\gamma \times Q \times V_1^2}{2g \times c^2}$$

The efficiency of a CFT will be defined as:

- Ratio of Brake Power to input power due to Head 'H'.

$$\eta = \frac{P}{P_i}$$

$$\eta = \frac{m \times \left[\left((V_1 \times \cos \alpha - u_1) \times \left(1 + \left(\psi \times \frac{\cos \beta_2}{\cos \beta_1} \right) \right) \right) \right] \times u_1}{\frac{\gamma \times Q \times V_1^2}{2g \times C^2}}$$

Simplifying the above equation, we get

$$\eta = \left(\frac{2C^2 \times u_1}{V_1} \right) \times \left(1 + \left(\psi \times \frac{\cos \beta_2}{\cos \beta_1} \right) \right) \times \left(\cos \alpha - \frac{u_1}{V_1} \right)$$

As the blade angles $\beta_1 = \beta_2$

$$\eta = \left(\frac{2C^2 \times u_1}{V_1} \right) \times (1 + \psi) \times \left(\cos \alpha - \frac{u_1}{V_1} \right)$$

It is clear that

$$\eta = f(u, V)$$

$$u = f(r, w)$$

r = Radius of Runner

w = Angular velocity of Runner

$$V = f(H)$$

So, $\eta = f(r, w, H)$

4. Results and Discussion

a. ANSYS Analysis

In the current study, the analysis is performed for the different edge profiles of blades for the turbine. The complete turbine is analyzed as the leading edges in the first stage of cross flow become trailing edges in the second stage of the cross flow turbine. For the optimization of blade profiles the second stage cannot be neglected as it has significant power output. For the determination of the most efficient leading and trailing edges, four possible blade profiles are made. The analysis procedure is shown Fig. 4 that consists of CAD model

development in CREO 3.0 and then mesh generation in ICEM CFD and finally simulation is carried out in the CFX. The detail methodology of ANSYS analysis is depicted in Fig. 5. In first step, CAD model is developed in the CREO and then CAD geometry is imported in ICEM to edit geometry and named the surfaces. Then mesh is generated and refined. Then the initial and boundary conditions are mentioned. Lastly, the model is solved in the CFX solver and results are generated.

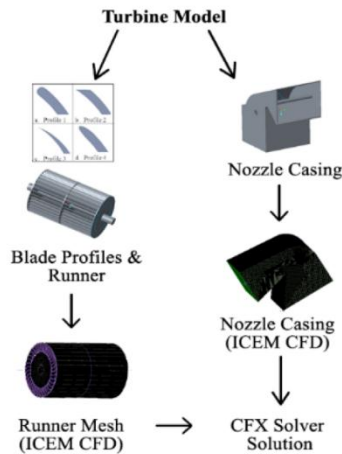


Fig. 4: Flow path for ANSYS

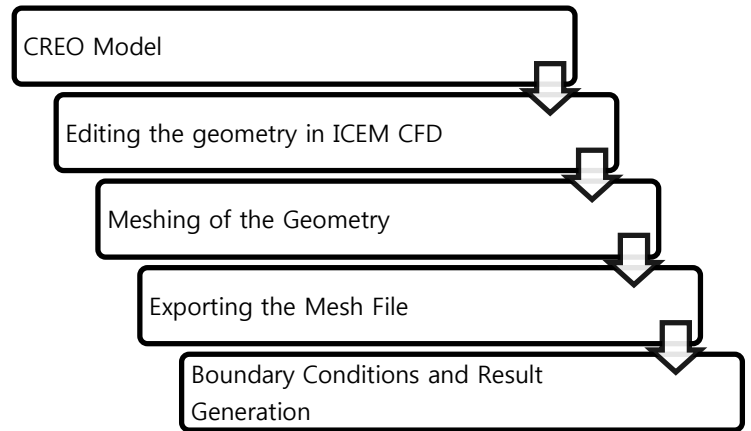


Fig 5: Ansys Methodology

b. Velocity Streamlines

Velocity streamlines and pressure contours were created in CFD-Post, the following are the results of the simulations. So for simplification we increased the outlet domain so that we have more accurate results and not affecting the geometry of design of the cross flow turbine.

Figures 6, Figure 7, Figure 8 and Figure 9 shows the streamlines in turbine for oval tip blades, round tip blades, pointed tip blades and flat tip blades, respectively. It shows an accurate description of flow in which velocity is increasing in the nozzle and decreasing as it exits the runner and the casing.

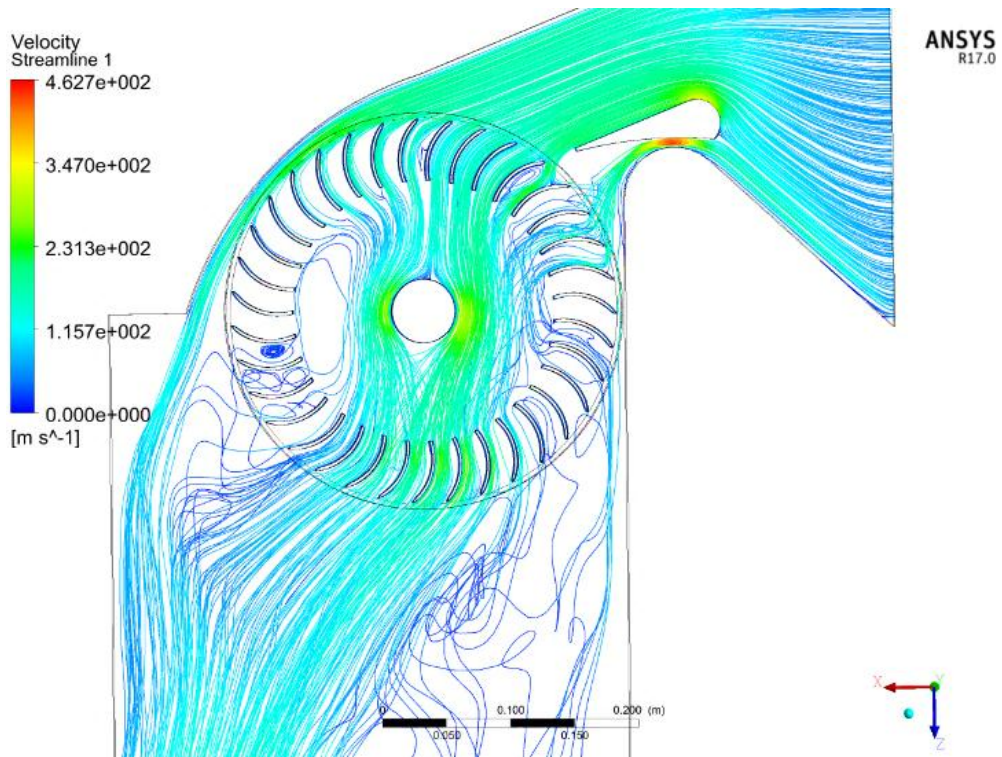


Fig. 6: Velocity streamlines for oval tip blades

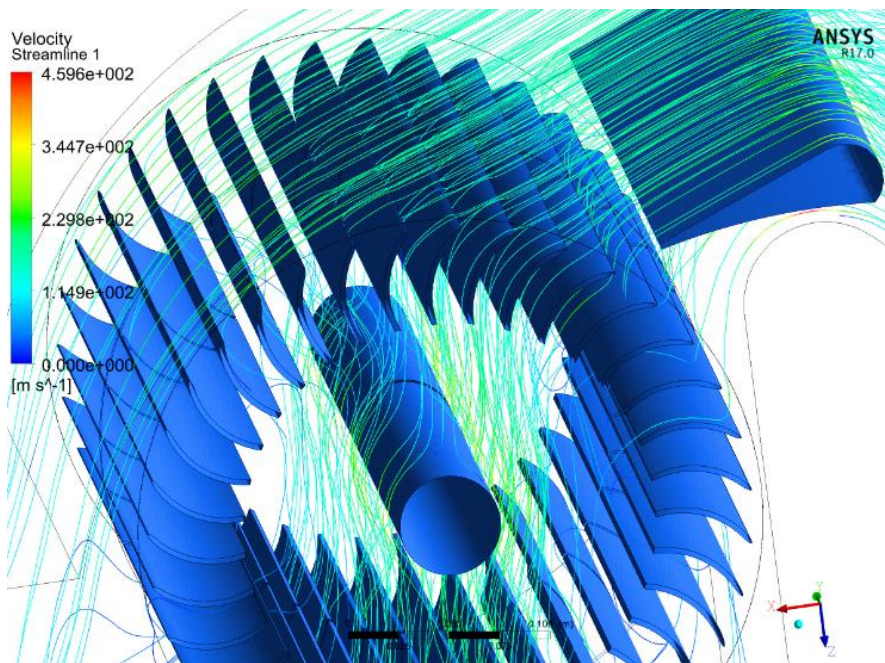


Fig. 7: Velocity streamlines for round tip blades

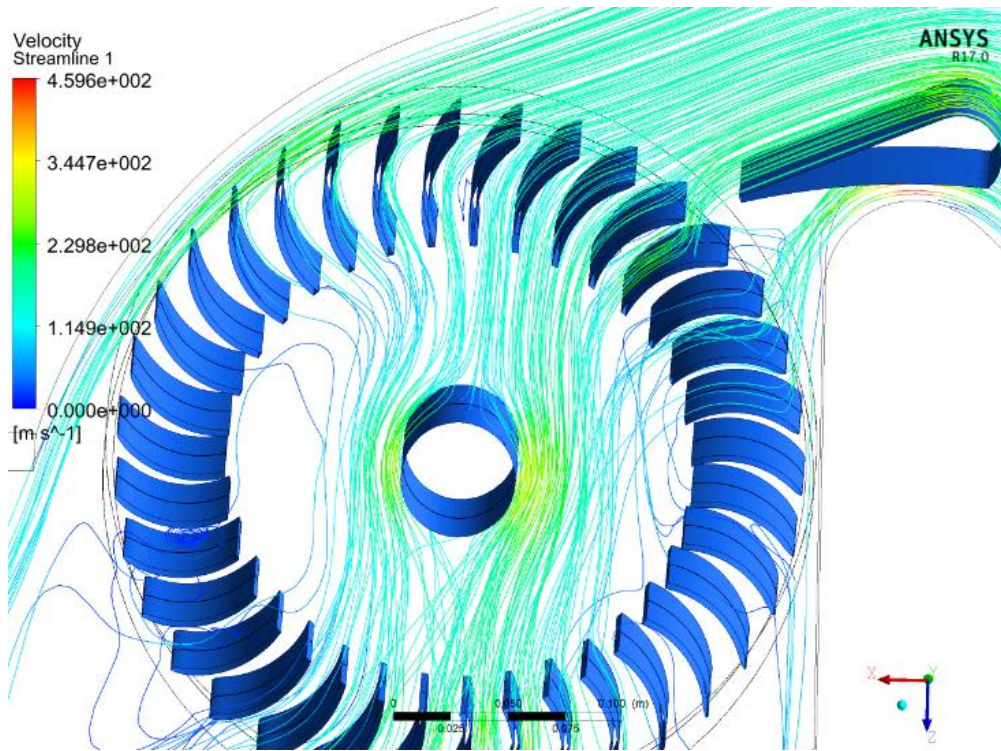


Fig. 8: Velocity streamlines for pointed tip blades

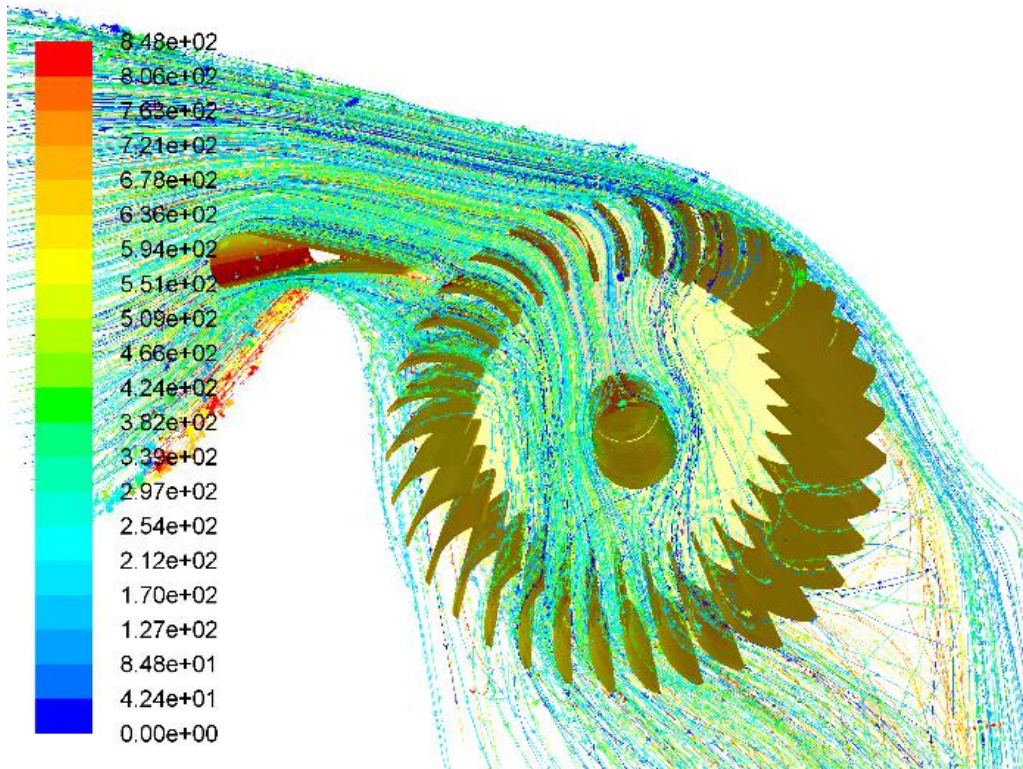


Fig. 9: Velocity streamlines for flat tip blades

c. Pressure Contours

The pressure contours show the variation of pressures along the CFT, pressure decreases as it passes through first stage and further decreases when it strikes the blades of second stage as shown in Fig. 10 for oval tip blades, Fig. 11 for pointed tip blades, Fig. 12 for round tip blades and Fig. 13 for flat tip blade.

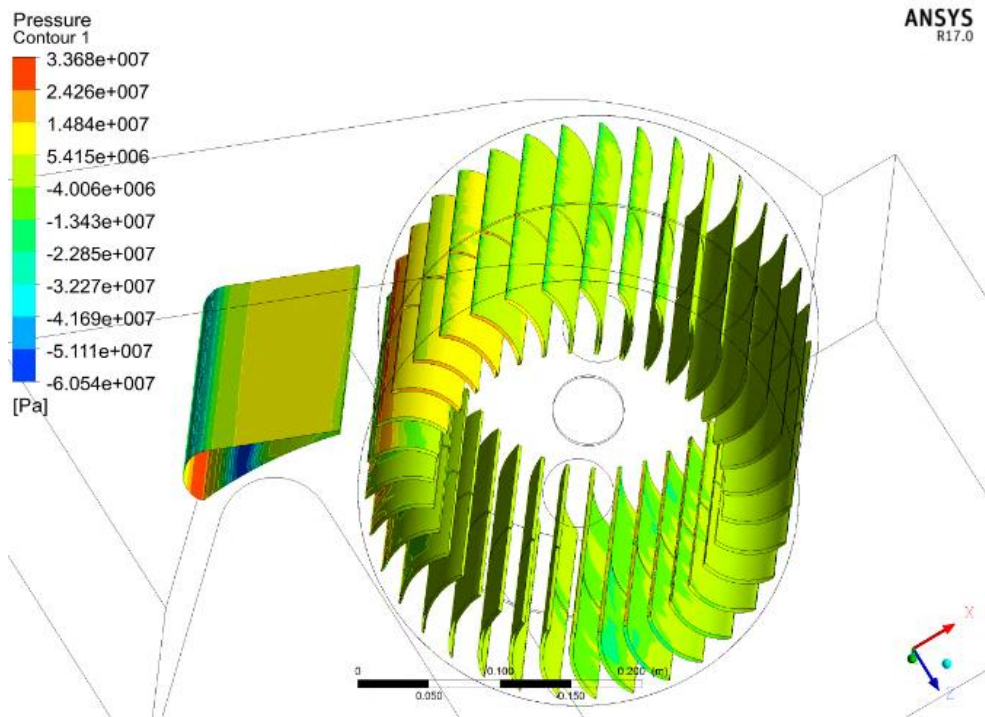


Fig. 10: Pressure contours for oval tip blades

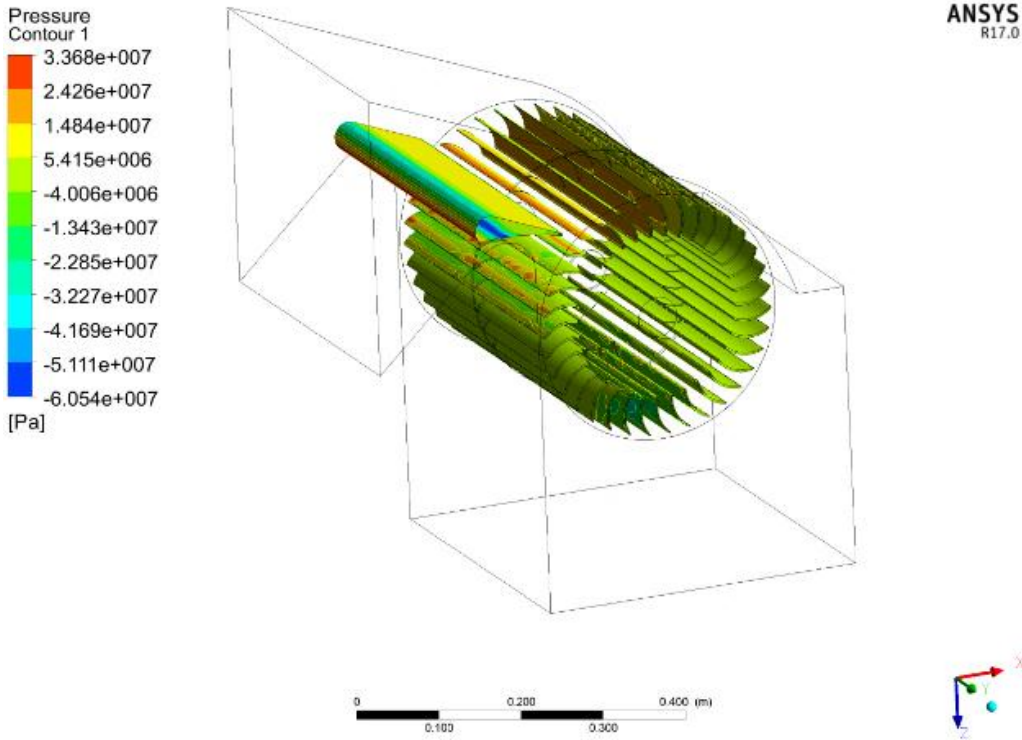


Fig. 11: Pressure contours for pointed tip blades

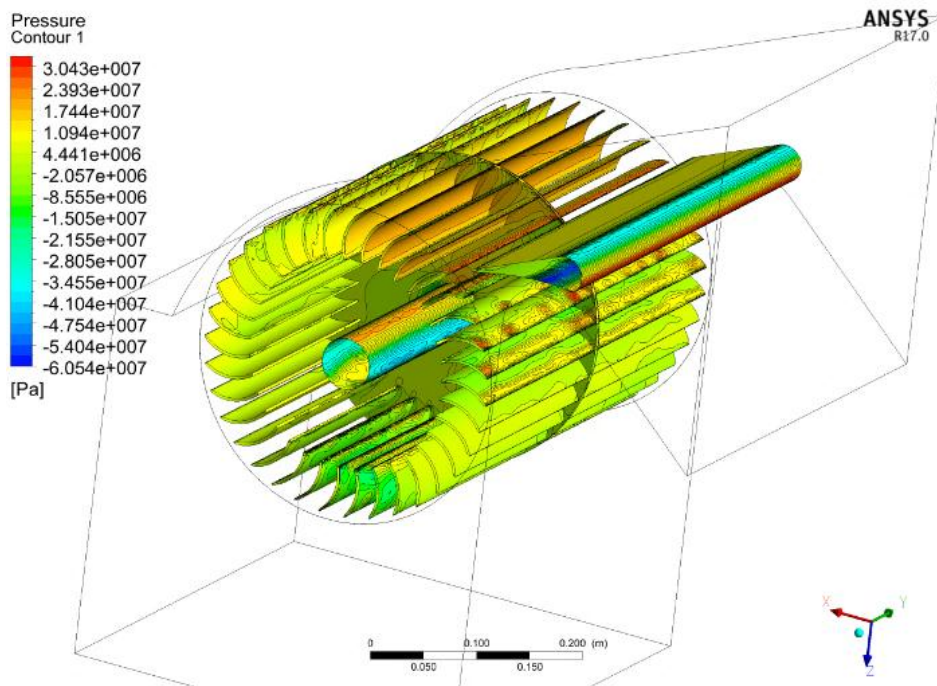


Fig. 12: Pressure contours for round tip blades

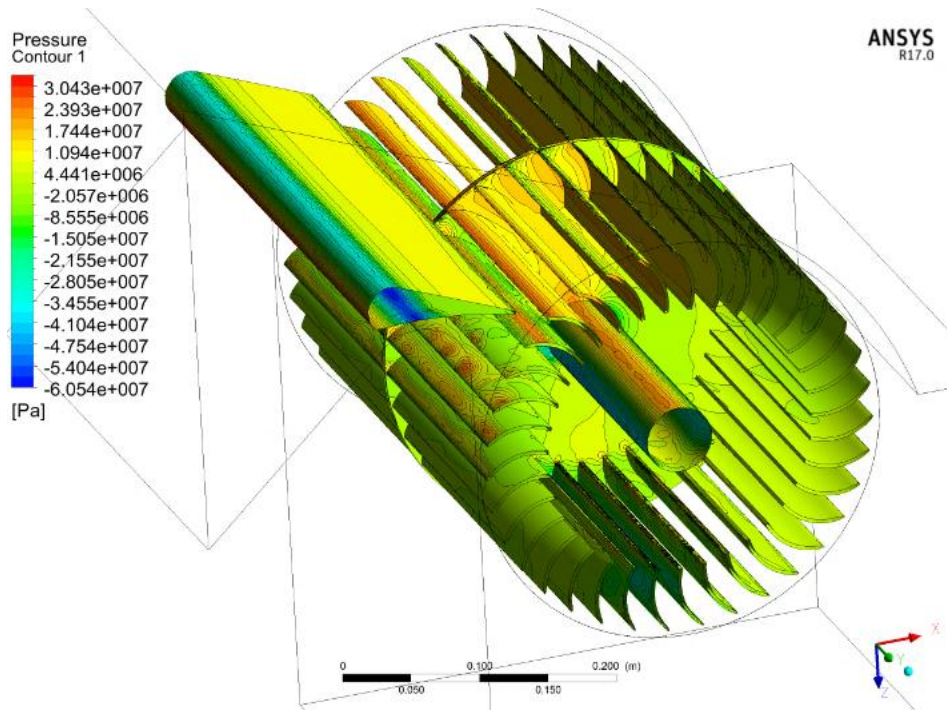


Fig. 13: Pressure contours for flat tip blades

d. Efficiency Comparison

The simulation was run for the complete turbine and the speed (rpm) was kept constant. All the profiles were simulated and tested to elaborate comparison between each profile. The simulation for the four different profiles with the same boundary conditions was done and their results for the simulation were analyzed. The results gave us the torque and using torques, efficiencies for each of the profile was calculated. The comparison of these profiles was done based upon the efficiency. And the conclusion was made regarding which profile is to be used to increase the performance of the turbine. The comparison of the efficiencies for four different blade profiles is shown in table 3.

The formulae used for the calculation of efficiencies using total pressure and torque from the ANSYS Results are as follows.

$$\text{BHP} = \text{Torq} \times \omega$$

$$\text{Torq} = \text{torque}_z()@ \text{Blade}$$

$$\omega = \text{Angular Velocity}$$

$$W = 2 \times 3.142 \times N/60$$

$$IHP = TP \times m_{dot}/1000$$

$$TP = \text{massFlowAve (Total Pressure) @CASE_IN}$$

$$m_{dot} = \text{massFlow()}@CASE_IN$$

$$\eta = BHP/IHP \times 100$$

Incorporating the above formulae gave us the following the following results for the four Blade Profiles.

Table 3: Efficiency (η) of different blades profiles at 386 rpm.

	Efficiency
Profile 1 (Round tip)	58.9 %
Profile 2 (Flat tip)	43.8 %
Profile 3 (Pointed tip)	51.4 %
Profile 4 (Oval tip)	53.5%

5. Conclusion

In this study, cross flow turbine was modeled in CAD CREO software and then simulated in ANSYS-CFX to compare the performance of the CFT for four different blade profiles in terms of their efficiency. The pressure and velocity profiles of four different profiles were computed using CFD tools and then efficiency of four types of profiles were compared. The results showed that efficiency of the profile-1 (round tip blade) is maximum at same boundary conditions.

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Appendix

Nomenclature

B – Nozzle thickness

D, D₁ – External Diameter of Blade

S_o - Thickness of jet

H - Head

N'_{sp} - Specific Speed

t - Blade spacing

HP_{out} - Output Power

u_1 - Tangential velocity of Blade outer edge
 n - Number of blades
 Q - Flow Rate
 v_1 - Relative velocity of entering water jet
 S_1 - Tangential blade positioning
 u_1' - Tangential velocity of Blade inner edge
 V_1 - Inlet water jet Absolute velocity
 V_2' - Absolute velocity of water from first stage exit
 v_1' - Relative velocity of entering water jet (2nd Stage)
 y_1 - Distance of jet from center of shaft
 y_1 - Distance of jet from inner periphery of the runner
 P_t - Theoretical Power Output
 V_1' - Absolute velocity of entering water jet (2nd Stage)
 h_t - Head Total
 D_2 - Inner Diameter of Runner
 v_2' - Relative velocity of the water from first stage exit
 HP_{in} - Input Horse Power
 C - Coefficient accounting for nozzle roughness
 V - Absolute velocity of water along the channel
 N - Angular speed of Runner
 a - Radial rim width

Greek Symbols:

η - System Mechanical Efficiency

α_2' - Angle between the runner inner periphery and absolute velocity of entering water jet
(1st Stage)

β_2 - Angle between the runner periphery and relative velocity of entering water jet (1st
Stage)

λ - Nozzle width ratio

ρ - Radius of blades curvature

α_1' - Angle between the runner inner periphery and absolute velocity of entering water jet
(2nd Stage)

β_1 - Angle between the runner periphery and relative velocity of entering water jet (2nd
Stage)

γ - Specific weight of water

Ψ - Coefficient accounting for blade roughness